

THE MILLIMETER-RADIO EMISSION OF BL LACERTAE DURING TWO γ -RAY OUTBURSTS

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Abstract: We present a study of the inexplicit connection between radio jet activity and γ -ray emission of BL Lacertae (BL Lac; 2200+420). We analyze the long-term millimeter activity of BL Lac via interferometric observations with the Korean VLBI Network (KVN) obtained at 22, 43, 86, and 129 GHz simultaneously over three years (from January 2013 to March 2016); during this time, two γ -ray outbursts (in November 2013 and March 2015) can be seen in γ -ray light curves obtained from *Fermi* observations. The KVN radio core is optically thick at least up to 86 GHz; there is indication that it might be optically thin at higher frequencies. To first order, the radio light curves decay exponentially over the time span covered by our observations, with decay timescales of 411 ± 85 days, 352 ± 79 days, 310 ± 57 days, and 283 ± 55 days at 22, 43, 86, and 129 GHz, respectively. Assuming synchrotron cooling, a cooling time of around one year is consistent with magnetic field strengths $B \sim 2 \mu\text{T}$ and electron Lorentz factors $\gamma \sim 10000$. Taking into account that our formal measurement errors include intrinsic variability and thus over-estimate the statistical uncertainties, we find that the decay timescale τ scales with frequency ν like $\tau \propto \nu^{-0.2}$. This relation is much shallower than the one expected from opacity effects (core shift), but in agreement with the (sub-)mm radio core being a standing recollimation shock. We do not find convincing radio flux counterparts to the γ -ray outbursts. The spectral evolution is consistent with the ‘generalized shock model’ of [Valtaoja et al. \(1992\)](#). A temporary increase in the core opacity and the emergence of a knot around the time of the second γ -ray event indicate that this γ -ray outburst might be an ‘orphan’ flare powered by the ‘ring of fire’ mechanism.

Key words: galaxies: active — BL Lacertae objects: individual (BL Lacertae) — galaxies: jets — techniques: interferometric — radio continuum: galaxies

1. INTRODUCTION

Certain active galactic nuclei (AGN) show prominent jets, powerful plasma outflows from the immediate environment of the central black hole. Jets are luminous emitters of synchrotron radiation which originates from the interplay of relativistic electrons and magnetic fields with complex structure (see, e.g., [Hughes 1991](#); [Böttcher et al. 2012](#)). Propagating disturbances, especially shocks, are supposed to play an important role in the observed variability of jets ([Hughes et al. 1985](#); [Marscher et al. 2008](#)). Blazars, a subclass of AGN marked by relativistic outflow speeds, high luminosities, and strong variability, are obvious candidates to explore the nature of AGN jets. Blazar jets are oriented close to the line of sight, thus causing substantial Doppler boosting. Typically, blazar jets radiate non-thermal emission over the wide

spectral range from radio to γ -rays. A typical spectral energy distribution (SED) consists of two ‘humps’: one which is located at relatively low frequencies from radio to UV which is attributed to synchrotron radiation; one at higher frequencies all the way up to γ -rays which is attributed to inverse Compton (IC) radiation (e.g., [Ramakrishnan et al. 2015](#)). To date, key physical processes in blazar jets, such as the acceleration of relativistic electrons, the structure of the inner jet region, the magnetic field structure, the origin of the seed photons for the IC process, and multi-waveband correlations are still unclear.

Broadly, blazars can be sub-divided into BL Lacertae (BL Lac) objects and flat-spectrum radio quasars (FSRQs), using the strength of broad emission lines, the synchrotron peak frequencies of their SEDs, and the shape of the spectral continuum as distinctive criteria. Even though, all blazar sub-classes can be understood

as members of a continuous blazar sequence (Ghisellini et al. 1998, Fossati et al. 1998; but see also Padovani 2007, Giommi et al. 2012). In this picture, the two peak frequencies of the synchrotron and IC components are connected to each other and show an anti-correlation with bolometric luminosity (the power of the jet) (e.g., Fossati et al. 1998).

The connection between radio and γ -ray emission in blazars is a matter of ongoing debate (Jorstad et al. 2001a; Marscher et al. 2010, 2011; Chatterjee et al. 2012; Raiteri et al. 2013; Marscher 2014; Ramakrishnan et al. 2016; Wehrle et al. 2016). On the one hand, it has been reported that γ -ray outbursts occur during the rising or peaking state of mm-radio flares (the “radio counterparts”) (Valtaoja & Teräsanta 1995; León-Tavares et al. 2011). The ejection of new jet components and γ -ray outbursts are correlated and tend to cause an increase in core opacity (Jorstad et al. 2001b, 2013). In addition, Jorstad et al. (2001a) found a positive correlation between radio core flux and γ -ray flux in 42 γ -ray bright blazars; this suggests that the γ -ray emission site is located near the core. León-Tavares et al. (2011) divided the vicinity of the radio core into the three regions – upstream, passing, and downstream of the core – to locate the γ -ray production site, and suggests possible scenarios for each case. On the other hand, several studies do not find significant correlations between radio and γ -ray emission from BL Lac objects (e.g., León-Tavares et al. 2011) and blazars (e.g., Max-Moerbeck et al. 2014). Hence, the connection between radio and γ -ray emission from blazar jets is rather obscure. The picture is complicated further by ‘orphan’ γ -ray flares that have no counterparts at lower frequencies (Krawczynski et al. 2004; Böttcher 2005; MacDonald et al. 2015; Banasiński et al. 2016). Orphan γ -ray flares are thought to occur occasionally in BL Lac objects and a few FS-RQs (Banasiński et al. 2016). A number of studies suggests possible origins of orphan flares: (i) a sudden enhancement of an external radiation field (e.g., from the accretion disk) (Krawczynski et al. 2004); (ii) a slow jet sheath (the ‘ring of fire’) in front of the radio core provides localized seed photons to a relativistic plasma cloud during its passage through the ring (MacDonald et al. 2015); (iii) an interaction of relativistic jet particles with a dense radiation field or stellar wind from a luminous star located around the central engine (Banasiński et al. 2016).

BL Lacertae (redshift $z = 0.069$, image scale 1.29 pc/mas), the prototypical BL Lac object, is characterized by strong flux variability from radio to γ -rays, high radio brightness (>1 Jy), superluminal motion of jet components, and linearly polarized emission. Villata et al. (2004) reported evidence for a (quasi-)periodic occurrence of major radio flares on a timescale of about eight years. BL Lac is known as a γ -ray bright AGN, beginning with the first detection of γ -ray emission by Catanese et al. (1997) in early 1995. Subsequent detections or reports occurred in 1997, 2005, 2011, 2012, and 2013 by Bloom et al. (1997), Albert et al. (2007), Arlen et al. (2013), Wehrle et al. (2016), and Gómez et al.

(2016), respectively. BL Lac was highly active at γ -ray and radio in 2012, showing a very strong radio outburst that peaked at the end of 2012 (see also Gómez et al. 2016; Wehrle et al. 2016, for recent discussions). Gómez et al. (2016) detected two polarized stationary features in the jet at 0.1 mas and 0.25 mas from the core, which they interpreted as recollimation shocks. Arlen et al. (2013) found a γ -ray flare in 2011 with a radio counterpart following four months later. Subsequently, Wehrle et al. (2016) confirmed that a γ -ray flare in 2012 is associated with the historic 2012 radio outburst, showing a time-lag of 3–5 months (again with the γ -ray emission leading the radio emission).

The Korean VLBI Network (KVN) is a dedicated mm-radio VLBI array with the unique capability of observing at four frequencies simultaneously (Lee et al. 2014). The KVN covers 22, 43, 86, and 129 GHz in frequency, and consists of three antennas with a maximum baseline length of 476 km. Systematic monitoring of blazar jets with multi-frequency simultaneous VLBI observations beyond 43 GHz is rare. Hence, the KVN will provide important information on variability, spectral properties, and evolution of blazar jets. We aim at exploring the connection between γ -ray and radio emission by monitoring the activity of the radio jet of BL Lac. In this study, we analyze the flux from and structure of BL Lac by employing dedicated KVN observations spanning three years in time, from January 2013 to March 2016; during this time, two γ -ray outbursts occurred.

In the following, we describe our data and observations in Section 2. In Section 3, we present the observational results, and we discuss the results in Section 4. Lastly, we summarize this paper in Section 5.

2. OBSERVATIONS AND DATA REDUCTION

We primarily use KVN VLBI data obtained within the interferometric MONitoring of GAMMA-ray BRIGHT AGN (iMOGABA) program.¹ iMOGABA monitors more than 30 γ -ray bright AGN via monthly (except during KVN maintenance times) KVN observations in single polarization (LCP) (Lee et al. 2016). iMOGABA uses a snapshot mode, with several 5-minute observations spread over a few hours for each target, resulting in total integration times of few tens of minutes per source. The first observation (iMOGABA1) was performed in December 2012, with observations going on ever since. More details about iMOGABA can be found in Lee et al. (2013); Algaba et al. (2015); Hodgson et al. (2016); Lee et al. (2016). As for the γ -ray activity of BL Lac, we follow the public database² (weekly light curve) of the *Fermi* Large Area Telescope (*Fermi*-LAT).

We collected data for BL Lac from 30 iMOGABA sessions (iMOGABA2 to iMOGABA32) from January 2013 (MJD 56308) to March 2016 (MJD 57448) for all four KVN frequencies. iMOGABA25 failed due to recording problems at Ulsan station. Due to technical

¹<http://radio.kasi.re.kr/sslee/>

²http://fermi.gsfc.nasa.gov/ssc/data/access/lat/ms1_1c/

Table 1
Summary of observations

Date	Session	Frequency ^a (GHz)	t_{obs}^b (min)
2013-01-16	iMOGABA2	22/43/86	25
2013-02-27	iMOGABA3	22/43/86/129	25
2013-03-28	iMOGABA4	22/43/86/129	20
2013-04-11	iMOGABA5	22/43/86/129	30
2013-05-08	iMOGABA6	22/43/86	25
2013-09-24	iMOGABA7	22/43	25
2013-10-15	iMOGABA8	22/43/86	20
2013-11-20	iMOGABA9	22/43/86/129	30
2013-12-24	iMOGABA10	22/43/86/129	35
2014-01-02	PAGaN	22/43	240
2014-01-27	iMOGABA11	22/43	35
2014-02-28	iMOGABA12	22/43/86/129	55
2014-03-05	PAGaN	86	109
2014-03-22	iMOGABA13	22/43/86/129	35
2014-04-22	iMOGABA14	22/43/86/129	35
2014-06-13	iMOGABA15	22/43	45
2014-09-01	iMOGABA16	22/43/86	30
2014-09-27	iMOGABA17	22/86	30
2014-10-29	iMOGABA18	22/43/86	30
2014-11-28	iMOGABA19	22/43/86	25
2014-12-26	iMOGABA20	22/43/86	40
2015-01-15	iMOGABA21	22/43/86	35
2015-02-24	iMOGABA22	22/43/86	35
2015-03-26	iMOGABA23	22/43/86/129	35
2015-04-30	iMOGABA24	22/43/86/129	35
2015-05-27	PAGaN	43/129	251
2015-09-24	iMOGABA26	22/43/86/129	30
2015-10-23	iMOGABA27	22/43/86	35
2015-11-01	PAGaN	22/86	250
2015-11-04	PAGaN	43	250
2015-11-30	iMOGABA28	22/43/86/129	35
2015-12-28	iMOGABA29	22/43/86/129	35
2016-01-13	iMOGABA30	22/43/86/129	40
2016-02-11	iMOGABA31	22/43/86/129	30
2016-03-01	iMOGABA32	22/43/86/129	30

^a Frequencies with successful imaging.

^b Total on-source time per session.

or weather issues, we could not always obtain a full set (i.e., 22–129 GHz) of images in an iMOGABA session. Occasionally, the 129-GHz band had to be excluded due to instrumental problems. Some sessions suffered from an insufficient uv coverage at some frequencies or missing baselines after data reduction; hence, we discarded those images. In order to increase the number of measurements over time and to perform a cross-check, we included five KVN observations executed independently by the Plasma-physics of Active Galactic Nuclei (PAGaN) project (Kim et al. 2015; Oh et al. 2015). PAGaN employs full-track dual-polarization observations of selected targets, typically reaching a few hours of integration time per source and per session. Due to different on-source times, the dynamic ranges of the PAGaN data at 22, 43, and 86 GHz are about 1.5–2 times higher than the corresponding iMOGABA data on average. At 129 GHz, only one PAGaN data set of poor quality was available; thus a meaningful comparison is not possible.

We summarize the iMOGABA and PAGaN observations in Table 1.

We reduced our data with the software packages AIPS³ and Difmap (Shepherd et al. 1994). We followed the standard AIPS steps for calibration of amplitudes and phases, bandpass, and opacity correction. To compensate for known amplitude losses, we multiplied a factor 1.1 to APARM(1) within the AIPS task APCAL (see Lee et al. 2015). Detecting and imaging our target in data obtained at 86 and 129 GHz proved difficult because of high levels of visibility phase noise. Due to atmospheric and instrumental effects, such as tropospheric errors caused by the inhomogeneous distribution of water vapor, and high receiver temperatures (e.g., Rioja & Dodson 2011; Martí-Vidal et al. 2012; Algaba et al. 2015; Rioja et al. 2015), it is challenging to obtain good signal-to-noise (S/N) ratios, well-aligned phases, and sufficient coherence times at those high frequencies.

In order to increase coherence times, we applied the frequency phase transfer (FPT) technique (Rioja & Dodson 2011; Algaba et al. 2015; Zhao et al. 2015; Hodgson et al. 2016) to parts of our data. Based on the assumption that the tropospheric path delay is independent of the observing frequency, we transferred phase solutions obtained for 43 GHz, scaled up by the ratio of frequencies, to the higher frequencies (86 and 129 GHz) by using the option XFER in the AIPS task SNCOR. We obtained improved coherence times of about five minutes on average (according to Algaba et al. 2015 and Rioja et al. 2015, coherence times longer than five minutes can be reached even at 129 GHz) and thus improved S/N. Using FPT for iMOGABA data was suggested to us after we had started our analysis (Algaba et al. 2015). Therefore, for iMOGABA2 to iMOGABA23, we applied FPT only to sessions with poor data quality at 86 and/or 129 GHz, and to all data after iMOGABA23. The difference in measured flux between data with and without FPT is within 5% at 86 and 129 GHz, in agreement with the statistical errors – meaning the application (or not) of FPT does not bias our flux measurements.

We imaged our radio data manually with Difmap, using CLEAN (Högbom 1974) deconvolution and phase self-calibration. (We could not apply amplitude self-calibration because the KVN consists of three antennas.) We derived positions, flux densities, and sizes of radio components by fitting circular Gaussian profiles to them. We estimated and propagated parameter errors as suggested by Formalont (1999) and Lee et al. (2008). Before imaging the uv data, we flagged outlying visibilities (showing up as down-streaming features in visibility amplitude – uv radius diagrams) for a given antenna whenever they were clearly caused by bad antenna pointings. As far as possible, we compared our imaging results to those from the VLBA–Boston University Blazar Monitoring Program⁴ as additional quality check. Our images showed the presence of a radio compo-

³ Astronomical Image Processing System, distributed and maintained by the National Radio Astronomy Observatory of the U.S.A. (<http://www.aips.nrao.edu/index.shtml>)

⁴ <http://www.bu.edu/blazars/VLBAproject.html>

nent (the ‘knot’) that corresponds to the jet. However, (re)detection of this component in the entire dataset proved difficult especially at the higher frequencies (cf. Figure 2). Each iMOGABA session observes simultaneously at 22, 43, 86, and 129 GHz for 24 hours, with 6 scans (corresponding to 30 minutes) on average for BL Lac, with only three antennas. The resulting sparse uv coverage leads to conspicuous side lobes and beam patterns that are (largely) identical in all four bands (when taking into account scaling with frequency), thus implying a risk of confusing artifacts with the actual radio jet. Therefore, we focus on analyzing the VLBI core in this study.

3. RESULTS

In this section, we present the multi-frequency behavior of BL Lac as obtained from our KVN data. During our observations, two γ -ray (0.1–300 GeV) outbursts occurred in November 2013 and March 2015. The first outburst, as well as its optical counterpart, was reported by Ramakrishnan et al. (2016) and Gómez et al. (2016). The second γ -ray outburst is visible in the data (their Figure 1) of Sandrinelli et al. (2017). Continuous data are provided by the weekly *Fermi*-LAT light curve⁵ (which is preliminary and used as a trigger for follow-up multi-wavelength observations). One can easily recognize the two outbursts in the *Fermi*-LAT light curve, peaking at 5.3×10^{-7} photons $\text{cm}^{-2} \text{s}^{-1}$ at around MJD 56620 and at 7.2×10^{-7} photons $\text{cm}^{-2} \text{s}^{-1}$ at around MJD 57110, respectively. The γ -ray flux remained on a high level continuously after the second outburst; this is different from the first outburst which lasted ~ 6 months.

3.1. Radio Morphology of BL Lac

In a typical KVN map, our observations show two radio components, the VLBI ‘core’ and a single ‘knot’ (in the standard nomenclature used by, e.g., Kadler et al. 2008) south of the core that corresponds to the well-known jet of BL Lac (e.g., Stirling et al. 2003). Figure 1 shows a KVN map of BL Lac at 22, 43, 86, and 129 GHz (with contours offset in right ascension to avoid overlap); this map is typical for our iMOGABA data when regarding contours starting at three times the rms noise level. The KVN cores of BL Lac at different frequencies (always at the map center) can be assumed to be identical; across our frequencies, core shift is less than about 0.2 mas (Dodson et al. 2017). The KVN core light curves (see Figure 2) are very similar in their structure, further supporting the conclusion that we observed the same structure at all frequencies. The location of radio knots is inversely proportional to the observing frequencies, with knots being located at roughly 3.4 mas, 1.8 mas, 0.9 mas, and 0.6 mas from the core at 22 GHz, 43 GHz, 86 GHz, and 129 GHz respectively. We expect the jet components of BL Lac at such distances to be optically thin (e.g., Denn et al. 2000). Hence, we concluded that our observations of the jet of BL Lac are heavily

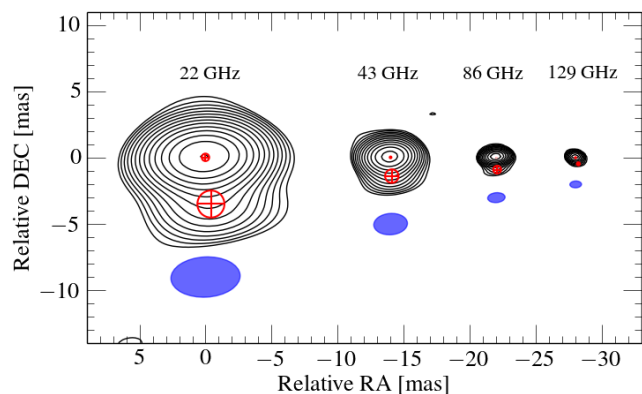


Figure 1. KVN total intensity maps of BL Lac at 22, 43, 86, and 129 GHz, from observation iMOGABA23 (cf. Table 1). To avoid overlap, contours are offset in RA. Identified radio components are marked with red \oplus symbols representing size and position as derived from fitting Gaussian circular profiles. Blue ellipses indicate the corresponding clean beams. Contour levels start at 1.1%, 1.9%, 2.41%, and 6.9% of the peak intensity at 22, 43, 86, and 129 GHz, respectively, and increase by factors $\sqrt{2}$.

influenced by sensitivity and uv coverage of KVN, forcing us to refrain from quantitative conclusions.

Qualitatively, we note that the jet appears longer at lower frequencies (cf. Figure 1). The same trend can also be found in O’Sullivan & Gabuzda (2009) and Abdo et al. (2011). This is a frequently observed feature of blazar jets which suggests that emission at lower frequencies originates from more extended regions in blazar jets (Valtaoja et al. 1992). In our case however, this observation is probably an artifact of the limited sensitivity of our KVN maps. The sensitivity decreases with increasing frequency, meaning that low-level flux contours are increasingly suppressed at higher frequencies.

3.2. Radio Light Curves

We monitored the flux densities of radio core and knot throughout our observing time as far as possible. Due to occasionally insufficient uv -coverage and/or high image noise, imaging of BL Lac or detection of the knot was not always possible at one or more frequencies. Especially, at 86 and 129 GHz we could detect a knot only in a few observations. Figure 2 shows the KVN multi-frequency light curves of BL Lac at 22, 43, 86, and 129 GHz. The light curves for all four frequencies follow very similar trends. The light curves of the core show relatively high flux levels, up to about 9 Jy, at the beginning and decay over time, reaching levels around 1 Jy at the end of our observations. We note that our observations cover the decay phase of the 2012 radio outburst (Wehrle et al. 2016). Flux densities of the knots are around 1 Jy at the beginning and decrease gradually by a factor of around two. We do not find obvious radio counterparts to the two γ -ray outbursts, even though any of the three local KVN core flux maxima located between the two γ -ray outbursts is a candidate for a counterpart to the first outburst.

⁵http://fermi.gsfc.nasa.gov/ssc/data/access/lat/msl_bc/source/BL_Lac

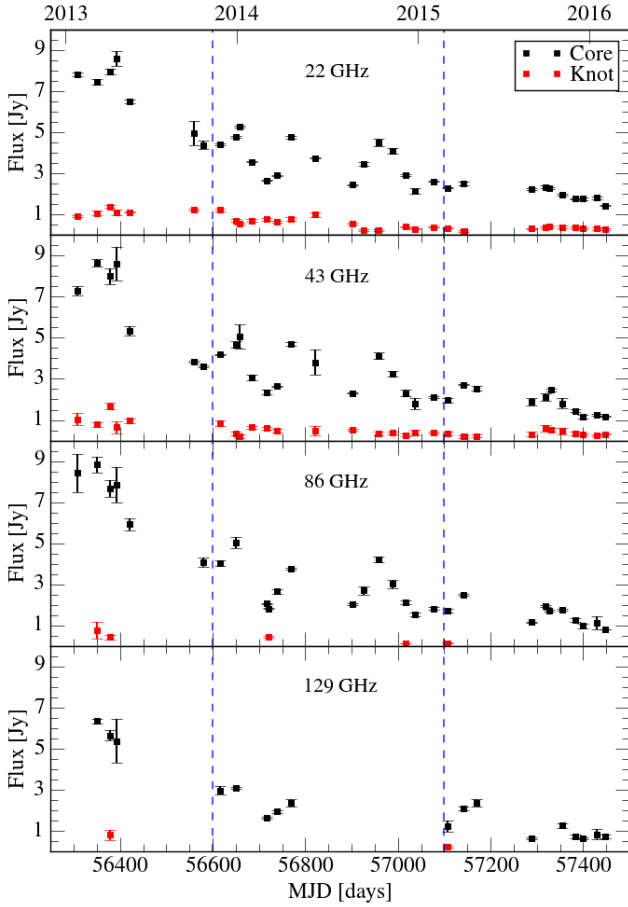


Figure 2. 22, 43, 86, and 129-GHz light curves of BL Lac obtained from KVN observations (both iMOGABA and PAGaN). The two blue dashed lines indicate γ -ray outbursts. Core (black) and knot (red) are plotted separately.

To provide a quantitative description of the long-term flux evolution of the core, we fitted exponential functions

$$S_\nu = A_\nu \exp(-B_\nu t) + C_\nu \quad (1)$$

with $B_\nu \equiv 1/\tau_\nu$ and τ_ν being the decay time scale at frequency ν , to each core light curve. Given that the intrinsic scatter of the data points about the long-term trend – AGN light curves show red-noise like variability patterns with smaller variability amplitudes at shorter time scales (Press 1978; recently, e.g., Park & Trippe 2017) – is much larger than their statistical errors, we applied uniformly-weighted least-squares minimization. Figure 3 illustrates the fitting results for the four light curves (omitting the actual data for clarity). At the very beginning of our observations, the fluxes at 22, 43, and 86 GHz are in good agreement; compared to these, the 129 GHz flux is lower by about 30%. Due to this, the flux density measurements at 129 GHz may not be robust and extra care should be taken when interpreting them and associated quantities. Later, fluxes are consistently higher at lower frequencies.

We obtain a decay timescale for each light curve from the exponential model. The timescales are 411 ± 85

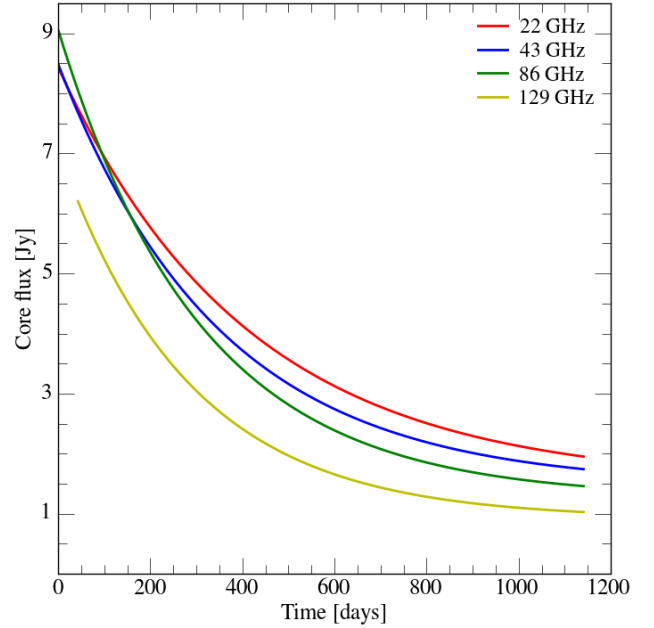


Figure 3. Exponential fits to the light curves of the core, quantifying the long-term flux evolution. Different colors indicate the four observing frequencies.

days at 22 GHz, 352 ± 79 days at 43 GHz, 310 ± 57 days at 86 GHz, and 283 ± 55 days at 129 GHz. The formal errors provided by the fits reflect the intrinsic short-term variability of the source fluxes rather than the actual statistical uncertainties. Taking this into account, we note that the decay timescale depends on the observing frequency. We fit a power-law to the timescale – frequency data and re-scale the error bars such that $\chi^2/\text{d.o.f.} = 1$. Figure 4 shows the resulting relation. The re-scaled errors on the timescales are ± 3.9 days at 22 GHz, ± 3.6 days at 43 GHz, ± 2.6 days at 86 GHz, and ± 2.5 days at 129 GHz. The best-fit line returns a power-law index of -0.208 ± 0.007 . Using a linear approximation for the frequency range covered by our data (and applying, again, error re-scaling), we find a slope of -1.05 ± 0.23 day/GHz – in other words, for each additional GHz in frequency, the decay timescale drops by about one day in the frequency range 22–129 GHz.

3.3. Spectral Indices and Spectrum of the Core

We analyzed the evolution of the spectrum of the core in view of a possible evolution of its opacity, beginning with spectral indices from pairs of adjacent frequencies (“pairwise indices”). As mentioned in Section 2, we could not always obtain measurements for all four frequencies, leading to different numbers of pairwise indices for the three frequency pairs. Due to the small time gap of three days between them, we treated the PAGaN observations of MJD 57327 and 57330 (2015 November 1 and 4) as a single measurement. We defined the spectral index α via $S_\nu \propto \nu^\alpha$, where S_ν is flux density of the core and ν is observing frequency. We adopt the conventional

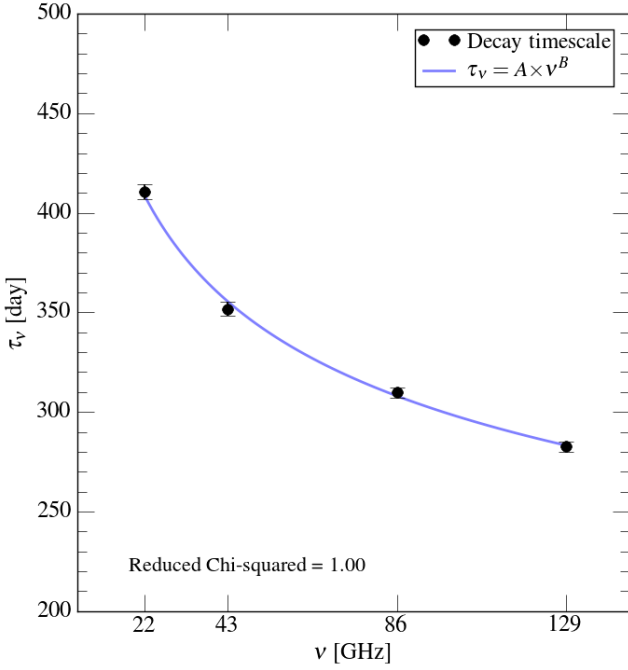


Figure 4. Decay timescale of the core flux as function of observing frequency. Both axes are linear. Errors have been re-scaled such that $\chi^2/\text{d.o.f.} = 1$. The blue solid line represents the best power-law fit, with a power-law index of -0.208 ± 0.007 .

criterion that spectra with $\alpha < -0.5$ and $\alpha > -0.5$ are ‘steep’ and ‘flat’, respectively (e.g., [Orienti et al. 2007](#); [Netzer 2013](#)). Figure 5 shows the pairwise spectral indices of the core as function of time. We obtained 31 spectral index values with an average value of -0.17 at 22–43 GHz, 27 indices with an average value of -0.14 at 43–86 GHz, and 16 indices with an average value of -0.89 at 86–129 GHz. Our observations show for the first time explicitly that the VLBI core of BL Lac is optically thick at frequencies higher than 43 GHz over several years. This agrees with expectations that the core should be optically thick because of synchrotron self-absorption (SSA) ([Denn et al. 2000](#); [Wehrle et al. 2016](#)). The spectral indices for the range from 22 to 86 GHz slightly decrease with time, in agreement with the trend illustrated by Figure 3. Figure 5 shows indication for a steady spectral hardening at 43–86 GHz from $\alpha \approx -0.3$ to $\alpha \approx -0.1$ for a few months around the time of the second γ -ray event, just after a rapid spectral softening. For the frequency pair 86–129 GHz, we see indication for the core becoming optically thin at these high frequencies; given the large errors, this conclusion has to be handled with care however.

Given that KVN provides multi-frequency data sets, we can obtain mm-wavelength spectra that are more sophisticated than the use of pairwise spectral indices. Whenever possible, we fit a power-law to spectra of the core consisting of the flux data that were obtained simultaneously at 22, 43, 86, and 129 GHz, thus making the standard assumption that BL Lac shows a synchrotron

Table 2
Spectral indices of the core as function of time

MJD ^a	α_{22-43}	α_{43-86}	α_{86-129}	α_{22-129}^c
56308	-0.11 ± 0.05	0.21 ± 0.17		
56350	0.22 ± 0.04	0.03 ± 0.07	-0.83 ± 0.12	-0.04 ± 0.13
56379	0.01 ± 0.07	-0.06 ± 0.10	-0.76 ± 0.17	-0.14 ± 0.09
56393	0.00 ± 0.15	-0.13 ± 0.21	-0.96 ± 0.57	-0.20 ± 0.11
56420	-0.28 ± 0.06	0.15 ± 0.09		
56559	-0.36 ± 0.17			
56580	-0.28 ± 0.07	0.17 ± 0.08		
56616	-0.08 ± 0.02	-0.05 ± 0.05	-0.77 ± 0.19	-0.17 ± 0.08
56650	-0.03 ± 0.05	0.11 ± 0.09	-1.22 ± 0.14	-0.14 ± 0.15
56659	-0.06 ± 0.17			
56684	-0.21 ± 0.06			
56716	-0.18 ± 0.08	-0.19 ± 0.08	-0.57 ± 0.10	-0.24 ± 0.04
56721				
56738	-0.14 ± 0.02	0.01 ± 0.06	-0.77 ± 0.13	-0.17 ± 0.08
56769	-0.02 ± 0.03	-0.32 ± 0.03	-1.15 ± 0.20	-0.30 ± 0.13
56821	0.02 ± 0.23			
56901	-0.08 ± 0.03	-0.19 ± 0.05		
56927				
56959	-0.12 ± 0.08	0.03 ± 0.07		
56989	-0.33 ± 0.08	-0.10 ± 0.11		
57017	-0.33 ± 0.10	-0.12 ± 0.12		
57037	-0.26 ± 0.25	-0.24 ± 0.25		
57077	-0.31 ± 0.03	-0.21 ± 0.07		
57107	-0.23 ± 0.08	-0.20 ± 0.11	-0.83 ± 0.55	-0.30 ± 0.06
57142	0.11 ± 0.06	-0.12 ± 0.03	-0.44 ± 0.11	-0.09 ± 0.07
57169				
57289	-0.24 ± 0.14	-0.69 ± 0.14	-1.57 ± 0.19	-0.56 ± 0.15
57318	-0.15 ± 0.14	-0.13 ± 0.14		
57327	0.10 ± 0.05	-0.52 ± 0.05		
57330 ^b	0.10 ± 0.05	-0.52 ± 0.05		
57356	-0.10 ± 0.21	-0.04 ± 0.21	-0.85 ± 0.28	-0.19 ± 0.09
57384	-0.29 ± 0.06	-0.18 ± 0.12	-1.45 ± 0.33	-0.38 ± 0.12
57400	-0.62 ± 0.13	-0.23 ± 0.21	-1.04 ± 0.36	-0.51 ± 0.08
57429	-0.56 ± 0.07	-0.11 ± 0.40	-0.76 ± 1.03	-0.40 ± 0.07
57448	-0.29 ± 0.05	-0.53 ± 0.05	-0.24 ± 0.26	-0.39 ± 0.04

^a Same dates as in Table 1 in units of MJD.

^b Quasi-simultaneous with the data of MJD 57327.

^c Spectral index using 22, 43, 86, and 129-GHz data.

spectrum like all radio-loud AGN (e.g., [Rani et al. 2011](#); [Trippe et al. 2011](#)). Figure 6 illustrates the estimation of a spectrum and shows the evolution of the spectral index α as function of time. We obtained 16 spectra in total. As expected from the pairwise spectral indices, BL Lac’s core spectrum is flat (within errors) at the beginning and steepens slightly throughout our observations, down to $\alpha \approx -0.5$. We summarize all spectral indices in Table 2.

4. DISCUSSION

The behavior of multi-waveband light curves provides important clues on the physical processes within blazar jets. Even though opacity and flux evolution depend on frequency, correlations between the flux variability at γ -rays and that at lower frequencies have been observed in blazar jets (as noted in Section 1). Unfortunately, there is no clear picture as yet: observed correlations (or the absence thereof) seem to change over time and from

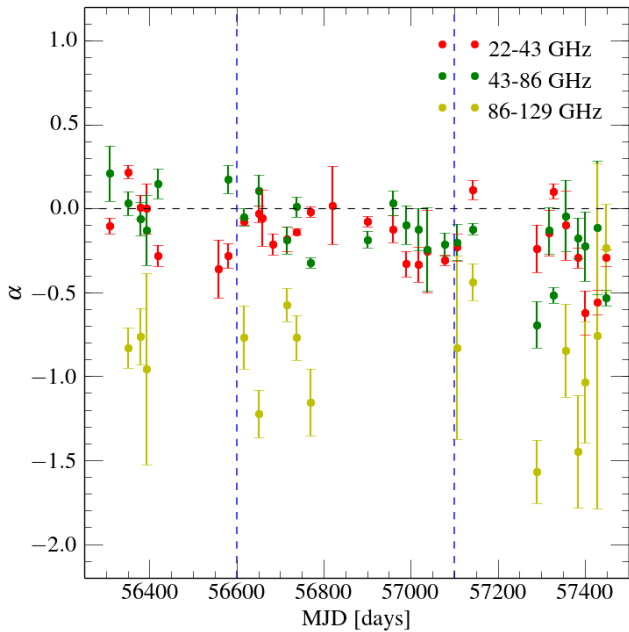


Figure 5. Pairwise spectral indices of the core as function of time, for the frequency pairs 22–43 GHz, 43–86 GHz, and 86–129 GHz. Different colors correspond to different frequency pairs. Vertical blue dashed lines mark the occurrence times of the two γ -ray outbursts.

source to source (e.g., Marscher 2014). Simultaneous multi-frequency observations by KVN may shed light on the connection between γ -ray emission and emission at high radio frequencies (up to ~ 130 GHz in our case). In this Section, we discuss the long-term decay of the 2012 radio outburst, the nature of the KVN core, and the connection between the two γ -ray outbursts and radio jet.

4.1. Variability and Cooling Time Scales

We find the highest fluxes for BL Lac right at the beginning of our observations. Wehrle et al. (2016) reported a strong outburst of BL Lac at 1.3 mm (225 GHz) at the end of 2012 preceded by strong γ -ray flaring. Accordingly, we may identify the 2012 radio outburst with the radio counterpart of the γ -ray flare(s) of the same year. Arguably, our observations cover the decay phase of the 2012 radio flare (see also Gaur et al. 2015). An exponential decay of radio luminosity is a common characteristic of blazar flares (Valtaoja et al. 1999; León-Tavares et al. 2011; Trippe et al. 2011; Chatterjee et al. 2012; Marscher 2014; Guo et al. 2016; Park & Trippe 2017). Unfortunately, our observations do not cover the rising stage of the radio outburst. Typically, the decay timescale of a flare in a radio AGN is about 1.3 times longer than its rise timescale (Valtaoja et al. 1999). This suggests rise timescales of ~ 316 days at 22 GHz, ~ 271 days at 43 GHz, ~ 238 days at 86 GHz, and ~ 218 days at 129 GHz.

The radio core of blazar jets is usually a compact, unresolved, and flat spectrum source that emits synchrotron radiation with high power. The radio core is

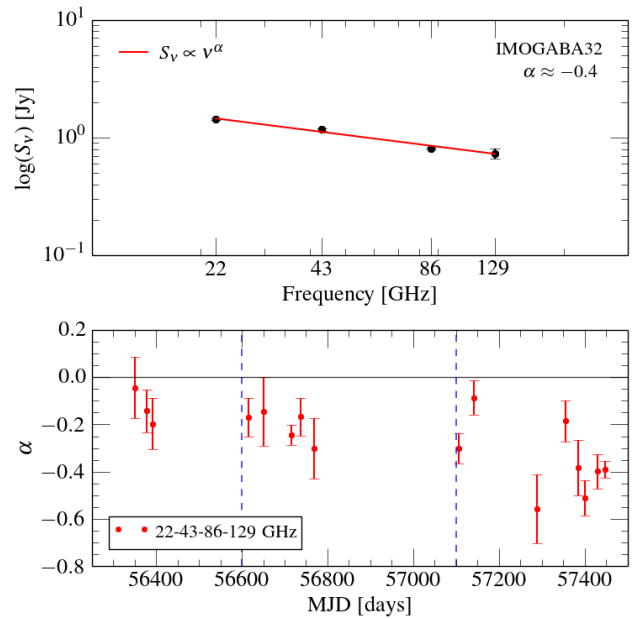


Figure 6. Radio spectra of the core from power-law fits to 22, 43, 86, and 129-GHz flux values. *Top:* An example spectrum, from data set iMOGABA32. *Bottom:* Spectral index α as function of time. Vertical blue dashed lines mark the occurrence times of the two γ -ray outbursts.

known to be located a few parsecs downstream from the central engine (León-Tavares et al. 2011). As noted by Spada et al. (2001), synchrotron radiation is the main cooling mechanism for relativistic electrons in blazar jets at such distances from the central engine, while IC dominates inside the broad line region ($\sim 10^{15}$ m). Here, we assume synchrotron cooling to be the dominant cooling mechanism in the core region (Sokolov et al. 2004). (In general, inverse Compton losses are less important than synchrotron losses in a stationary synchrotron source; Pacholczyk 1970). A characteristic synchrotron cooling time can be defined via $\tau_{\text{cool}} = E/\dot{E}$, with the electron energy $E = \gamma mc^2$ (with Lorentz factor γ , electron mass m , and speed of light c) and $\dot{E} = dE/dt$ (with time t) being the power radiated by a gyrating electron (e.g., Rybicki & Lightman 1997). In SI units and after transforming to the observer frame, the cooling time is

$$\tau_{\text{cool}} = 7.74 \left[\frac{\delta}{1+z} \right]^{-1} B^{-2} \gamma^{-1} \text{ seconds} \quad (2)$$

where B is the magnetic field strength, δ is the Doppler factor, and z is the redshift. For BL Lac, $z = 0.069$ and $\delta \approx 7$ (Hovatta et al. 2009). Cooling times on the order of one year (assuming $\tau_{\text{cool}} \approx \tau_{\nu}$; see Section 3.2) can be translated to $B \sim 2 \mu\text{T}$ and $\gamma \sim 10000$ which is consistent with the typical blazar magnetic field of $B \sim 1 - 10 \mu\text{T}$ (Lewis et al. 2016). Moreover, Agarwal et al. (2017) obtained the magnetic field of the BL Lac core at 4.8, 8, 14.5, and 22.2 GHz. They found B to increase with frequency, with $B \sim 1 \mu\text{T}$ at 22 GHz on average. Electron Lorentz factors $\gamma \sim 10000$ are consistent with

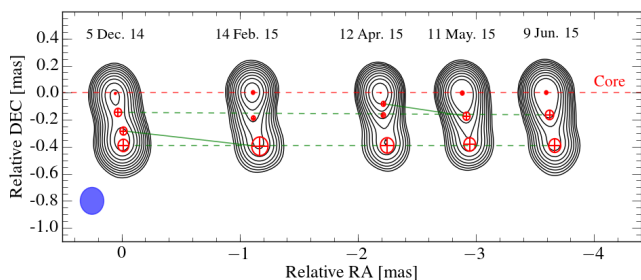


Figure 7. 43-GHz VLBA maps (from the BU data base) of BL Lac obtained around the time of the March 2015 γ -ray outburst. Contours represent total intensity levels ranging from 4% to 90.5% of the peak intensity. Red \oplus denote circular Gaussian components, the blue ellipse indicates the clean beam. Maps are shifted along the abscissa for clarity; all maps are restored with the same 0.2×0.2 mas beam.

the fact that the peak frequencies of the synchrotron and IC humps in BL Lac’s SED differ by about eight orders of magnitude (cf. Figure 27 of Wehrle et al. 2016).

The presence of longer decay time scales at lower frequencies, and the subsequent stratification of flux densities as function of frequency, might be an effect of longer synchrotron cooling times at lower electron energies (Marscher et al. 2008). In general, the synchrotron cooling time is longer at lower frequencies (Rybicki & Lightman 1997), which can be understood from the basic scaling relations of synchrotron radiation. An electron gyrating about a magnetic field line with angular frequency ω_B emits synchrotron radiation with a critical frequency $\nu_c \propto \gamma^3 \omega_B$ (e.g., Rybicki & Lightman 1997). With $\omega_B \propto \gamma^{-1}$, $\nu_c \propto \gamma^2$. Because $\tau_{\text{cool}} \propto \gamma^{-1}$ (Equation 2), the cooling time follows $\tau_{\text{cool}} \propto \nu_c^{-1/2}$ for *optically thin* plasmas. In addition, one needs to consider that electron energies commonly follow power-law distributions of the form $N(\gamma) \propto \gamma^p$ (with $p < 0$); as the cooling time is a function of γ , high-energy electrons will cool down faster. Accordingly, single-power laws are widely used to describe synchrotron losses in blazar jets (see also Böttcher et al. 2003; Sokolov et al. 2004).

In our case however, the KVN core of BL Lac is *optically thick* (cf. Section 3.3), meaning that observations at different frequencies probe different regions with different magnetic field strengths. In general, $B \propto d^{-1}$, with d being the distance from the central engine, in the VLBI core (Marscher 1995; Lobanov 1998). Marscher (1995) suggested that the observed γ becomes the maximum Lorentz factor for the given electron distribution, γ_{max} , at the VLBI core. We assume γ_{max} to be constant in the core region (e.g., Kaiser 2006). Our data (Section 3.2) follow a relatively shallow scaling relation $\tau \propto \nu^{-0.2}$. For a conical Blandford & Königl (1979) jet, different observing frequencies probe different plasma surfaces. This results in the well-known ‘core shift’ relation $d \propto \nu^{-1}$ (Lobanov 1998; but see also Agarwal et al. 2017). Such a scaling law is in tension with our observations: even for (approximately) constant values of γ , we would expect $B^2 \gamma \propto d^{-2} \propto \nu^2$ and thus $\tau \propto \nu^{-2}$ – which is much steeper than our observed relation.

An alternative explanation for our result is provided by the assumption that the millimeter radio core of BL Lac is a standing recollimation shock (Gómez et al. 1997; Marscher et al. 2008). Such a shock forms where the gas pressure in the jet does not match the gas pressure of the ambient interstellar medium (e.g., Cawthorne et al. 2013). Numerical simulations by Dodson et al. (2017) suggest that the radio core of BL Lac follows the usual core shift relation at centimeter wavelengths and coincides with a recollimation shock (which is optically thin) at millimeter wavelengths (see also Marscher 2012; Martí et al. 2016). In this picture, the recollimation shock is a physical structure at a fixed position; high frequency (mm to sub-mm) radiation may originate entirely from the shock. The core shift scaling starts to deviate from the relation $d \propto \nu^{-1}$ at wavelengths shorter than about one centimeter. At sufficiently high observing frequencies, the synchrotron radiation originates from the same plasma surface at all frequencies; the scaling of magnetic field strength with frequency breaks down, i.e., $B^2 \gamma$ and τ become independent of frequency. We suspect that the KVN frequency bands cover the frequency range where this transition occurs in BL Lac, probably between 86 and 129 GHz. This interpretation is supported by the astrometric observations of Dodson et al. (2017), who find that the core shift relation beyond ~ 30 GHz is much shallower than $d \propto \nu^{-1}$ – in agreement with the signature of a recollimation shock (see also Wehrle et al. 2016; Gómez et al. 2016). O’Sullivan & Gabuzda (2009) find the millimeter radio core of BL Lac to be located $\lesssim 0.5$ pc from the jet base.

4.2. Shock Evolution in the Core Region

The energy distribution of electrons in relativistic AGN jets is commonly assumed to follow a power law (Hughes et al. 1985; Ghisellini et al. 2002; Maselli et al. 2010; Rani et al. 2011; Trippe et al. 2011; Giommi et al. 2012; Karamanavis et al. 2016), resulting in power law synchrotron spectra – in agreement with our KVN data. Throughout our observations, the long-term evolution of the core spectrum follows the overall long-term evolution of the core light curves (cf. Figures 3 and 6). At the beginning, the spectrum is approximately flat ($\alpha \approx 0$) while the core flux is at its highest levels; over time, the flux decreases and the spectrum becomes steeper. A hardening of the spectrum at higher fluxes is a signature of powerful shocks and is consistent with the known flux evolution of BL Lac since the 2012 radio outburst (Ghisellini et al. 2002; Gaur et al. 2015; Wehrle et al. 2016). The subsequent behavior of the spectrum (i.e., becoming steeper) over time indicates again that the source underwent radiative energy losses by synchrotron radiation and Compton scattering (Blumenthal & Gould 1970). A physical explanation is provided by the ‘generalized shock model’ of Valtaoja et al. (1992) which links the evolution of a shock to the observable evolution of its turnover peak frequency. As the shock evolves with time, the turnover peak frequency of the spectrum moves to lower frequencies – in good agreement with our observations (Figure 6).

The KVN core is consistent with being optically thick at least up to 86 GHz (cf. Figures 5 and 6) throughout our observations. This is in contrast to the observation that the core becomes optically thin at mm-wavelengths occasionally due to the emission from newly ejected jet components (Hodgson 2015). This apparent conflict can probably be resolved by taking into account that the KVN core is a blend of multiple components that would be spatially resolved by higher-resolution observatories (see also Rioja et al. 2014, 2015; Zhao et al. 2015). The long-term steepening of the spectrum which we observe (Figure 6) might be caused by the jet emission becoming brighter relative to the core emission over time. This implies that the core spectrum might continue its steepening until a jet component is ejected, and then return to $\alpha \approx 0$. At 129 GHz, the KVN core may be optically thin permanently – as expected at sufficiently high frequencies. However, we cannot ignore possible instrumental effects of the KVN that can result in unwanted amplitude drops and which are supposed to be more severe at higher frequencies (Algaba et al. 2015; Lee et al. 2016).

4.3. The Radio – γ -Ray Connection

Radio and γ -ray light curves of blazars tend to be connected such that a γ -ray outburst precedes a radio outburst (Valtaoja & Teräsanta 1995; Jorstad et al. 2001b; Marscher et al. 2008, 2011; León-Tavares et al. 2011; Arlen et al. 2013; Raiteri et al. 2013; Max-Moerbeck et al. 2014; Ramakrishnan et al. 2015; Karamanavis et al. 2016; Wehrle et al. 2016). It has been suggested that a moving disturbance originating near the jet base produces flares both at radio and γ -rays as it propagates along the jet flow (Marscher et al. 2008; Max-Moerbeck et al. 2014). In this scenario, the γ -ray outburst is assumed to occur in the inner jet region (upstream of the radio core) where the jet is opaque at radio wavelengths; the radio outburst becomes observable once the disturbance has passed through the radio core region. To add complexity to this issue, observations indicate that the production site of γ -ray outbursts is located parsecs downstream of the radio core at least occasionally (e.g., León-Tavares et al. 2011). In addition, recent studies (e.g., Wehrle et al. 2016, Hodgson et al. 2017) found recollimation shocks in blazar jets within 0.5 mas downstream from the core, and suggested the recollimation shocks as a candidate of the origin of γ -ray outbursts in blazar jets.

The typical rise time of radio outbursts is on the order of one year (e.g., Hovatta et al. 2008). In blazars, the observed delays between γ -ray and radio outbursts range from hours to a few hundred days, with the γ -ray emission leading the radio emission (Arlen et al. 2013; Jorstad et al. 2013; Raiteri et al. 2013; Max-Moerbeck et al. 2014; Ramakrishnan et al. 2015; Wehrle et al. 2016). Accordingly, the identification of the radio counterparts to a specific γ -ray outburst is not straightforward if significant variability such as the multiple outbursts (the three minor radio flux peaks) after the first γ -ray event in Figure 2 is present in the radio light curve. In

our case, we do not find obvious radio counterparts to the two γ -ray outbursts.

The apparent absence of a radio – γ -ray correlation (like the absence of radio counterparts) in blazar jets or BL Lac objects has been noted before (Denn et al. 2000; León-Tavares et al. 2011; Orienti et al. 2013; Max-Moerbeck et al. 2014; Ramakrishnan et al. 2016). The lack of radio counterparts can result from radio and γ emission originating from different regions (e.g., León-Tavares et al. 2011); in this scenario, γ emission results from IC scattering near the core with seed photons from the accretion disk, the outflowing broad-line region (BLR), or the dusty torus. A complex variability pattern could cause a weak radio counterpart to be ‘buried’ under radio outbursts that are unrelated to the γ -ray emission. Indeed, already Valtaoja et al. (1999) noted that light curves of BL Lac are difficult to decompose into individual outbursts. Gaur et al. (2015) suggested geometry effects to be important, specifically variable Doppler boosting of the jet emission due to viewing angle changes. This might cause radio counterparts to be missed or underestimated.

Last but not least, the γ -ray outbursts of 2013 and 2015 might be ‘orphan’ events that show no correlation with the luminosity at longer wavelengths. An orphan γ -ray outburst was observed in the blazar PKS 1510-089 by Marscher et al. (2010); MacDonald et al. (2015) explained this outburst as the result of a disturbance passing through the inner jet region. To further complicate matters, BL Lac shows (apparent) radio counterparts to γ -ray outbursts at least in some cases (Arlen et al. 2013; Wehrle et al. 2016). Not only the light curves but also the evolution of the radio spectrum can be related to the γ -ray activity of blazars. For the quasar 3C 454.3, Jorstad et al. (2013) found that γ -ray outbursts coincide with increases in – spectroscopically determined – core opacity. As shown in Figure 5, the spectral index of BL Lac’s core at 43–86 GHz reaches a local minimum, with $\alpha \approx -0.3$, roughly two months before the second γ -ray outburst. From then on, the spectral index, and thus the core opacity, increases up to $\alpha \approx -0.1$ a few weeks after the γ -ray outburst. This can be explained by the passage of a newly ejected jet component through the core: while in the core region, the new component is obscured and temporarily increases (or dampens the long-term decrease of) the flux from the optically thick core, resulting in increased values of α . This interpretation is strengthened by the results of Arlen et al. (2013) who found a γ -ray outburst in June 2011 (at MJD 55711) to coincide with the ejection of a new jet component.

The connection between γ -ray outbursts and ejections of new components is a known feature of blazars (Marscher et al. 2010, 2011; Arlen et al. 2013; Jorstad et al. 2013; Gómez et al. 2016; Wehrle et al. 2016) which is, however, not a universally valid relation (Denn et al. 2000; Jorstad et al. 2001b). We used archival VLBA data from the BU data base to search for a new jet component in spring 2015; the maps are shown in Figure 7. Indeed, a new jet component might have appeared

about 0.1 mas south of the VLBA core in April 2015 which, however, only shows up in the April 2015 map – meaning we cannot claim the occurrence of a new jet component with sufficient certainty. If, indeed, a new jet component appeared in April 2015, this could explain the occurrence of an orphan γ -ray outburst in March 2015 via the ‘ring of fire’ mechanism (MacDonald et al. 2015). In this picture, an orphan γ -ray outburst arises from a relativistic plasma cloud moving through the inner jet region and precedes the emergence of a new radio jet component – by ~ 20 days in the case of PKS 1510-089, and possibly by a similar amount of time in case of BL Lac in 2015 (~ 25 days).

5. SUMMARY

We analyzed multi-frequency KVN radio data of BL Lac spanning three years, from January 2013 to March 2016 to study the connection between radio and γ -ray emission in blazar jets. We obtained light curves and spectra of the radio core at mm-wavelengths during a period when BL Lac showed two γ -ray outbursts that occurred in November 2013 and March 2015. We summarize our main results in the following.

1. Our observations cover the aftermath of the major radio flare that occurred in 2012. During the entire time of our observations, the radio flux from the KVN radio core decayed exponentially, and two γ -ray outbursts occurred in BL Lac. We found decay time scales τ of 411 ± 85 days (22 GHz), 352 ± 79 days (43 GHz), 310 ± 57 days (86 GHz), and 283 ± 55 days (129 GHz), with formal errors including intrinsic short-term variability. Assuming synchrotron cooling, such decay times are consistent with magnetic fields $B \sim 2 \mu\text{T}$ and electron Lorentz factors $\gamma \sim 10\,000$.
2. We find that the flux decay time scales with observing frequency like $\tau \propto \nu^{-0.2}$. This scaling law is much shallower than the synchrotron energy loss expected from optical depth effects in a Blandford & Königl (1979) jet. Therefore, we suspect the KVN radio core to be a standing recollimation shock (e.g., Marscher et al. 2008) – in agreement with independent recent astrometric observations (Dodson et al. 2017) of the core shift.
3. The radio core spectrum is initially flat ($\alpha \approx 0$) and steepens with decreasing flux, reaching $\alpha \approx -0.5$ at the end of our observations. This is in agreement with the ‘generalized shock model’ of Valtaoja et al. (1992) wherein the turnover peak moves to lower frequencies when the shock decays, with the shock corresponding to the 2012 radio flare.
4. There is no obvious radio counterpart to any of the two γ -ray outbursts covered by our study. Possible explanations are: (i) the γ -ray emission originates downstream of the core; (ii) the radio counterparts are masked by the complex intrinsic red-noise type variability; (iii) geometry effects like variations in Doppler boosting; (iv) there is actually no radio counterpart – i.e., the γ -ray outbursts are ‘orphans’.
5. The temporary increase in the core opacity two months before the second γ -ray outburst, as well as the outburst itself, might both be due to the emergence of a new jet component. The detection of a new VLBA radio knot in April 2015 tentatively suggests that the second γ -ray event might be an orphan γ -ray event powered by the ‘ring of fire’ mechanism.

Overall, our results strengthen the case for a causal connection between the radio and γ -ray activity in BL Lac, and potentially in blazars in general. Even though, we are still missing many important details. Future studies will need to explore if recollimation shocks are a general features of blazar jets; under which circumstances one may expect radio-flux counterparts to γ -ray outbursts; and which physical mechanism causes orphan γ -ray flares.

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